

Esercizi sui prodotti notevoli

$(a + b)^2 = a^2 + 2ab + b^2$	quadrato di un binomio
$(a + b + c)^2 = a^2 + b^2 + c^2 + 2ab + 2ac + 2bc$	quadrato di un trinomio
$(a + b)(a - b) = a^2 - b^2$	differenza di quadrati
$(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$	cubo di un binomio
$(a + b)(a^2 - ab + b^2) = a^3 + b^3$	somma di cubi
$(a - b)(a^2 + ab + b^2) = a^3 - b^3$	differenza di cubi

Semplificare le seguenti espressioni:

$$57. (a - 3b)(a + 3b)(a^2 + 9b^2) - 9(a^4 - 9b^4). \quad [-8a^4]$$

$$58. (a + b)(a - b) - a(a - 2b). \quad [2ab - b^2]$$

$$59. (p^2 + 1)(p + 1)(p - 1) - p^3(p - 1) + (1 - p)(p^2 + p + 1). \quad [0]$$

$$60. (2a + 1)^2 + (3a - 1)^2 - (a + 2)(a - 2) - 2(3 - a). \quad [12a^2]$$

$$61. (3b + 2a)(3b - 2a) + (3a - b)(3a + b) - 2(b - a)(a + b). \quad [7a^2 + 6b^2]$$

$$62. (x^2 + 1)(x + 1)(x - 1) - x^3(x - 1) + x - (x - 1)(x^2 + x + 1). \quad [x]$$

$$63. (x^2 - xy + y^2)(x^2 + xy + y^2) - x^2(x^2 + y^2). \quad [y^4]$$

$$64. (x + y)(x^2 - xy + y^2) + (x - y)(x^2 + xy + y^2). \quad [2x^3]$$

$$65. 3(t - 1) + (t^2 - 1)(t^2 + 1) - t(t^3 + 3). \quad [-4]$$

$$66. (a + 1)(a + 2)(a + 3) - (a + 1)(a + 2) - a^3 - 4(2a + 1). \quad [5a^2]$$

$$67. 3(a + 2b)^2 - 2(a + 2b)(a - 2b) + (a - 2b)^2 - 8b(a + 2b). \quad [2a^2 + 8b^2]$$

$$68. (2x + 3y)^2 - \left(\frac{1}{2}x + \frac{1}{3}y\right)^2 + (2x - 3y)^2 - \frac{31}{4}x^2 - \frac{161}{9}y^2. \quad \left[-\frac{1}{3}xy\right]$$

$$69. (x^2 + x + 1)(x^2 - x + 1) - x^2(x^2 + 1) + (x + 1)(x - 1). \quad [x^2]$$

$$70. (x^6 + 1)(x^2 - 1)(x^4 + x^2 + 1) - (x^4 - 1)^3 - 3x^8. \quad [-3x^4]$$

$$71. (2p - 5q)(2p + 5q) + (p - 3q)^2 + (p + 4q)(-p + 4q). \quad [4p^2 - 6pq]$$

$$72. (a + b)^2 - (a - b)^2 + a(a - 4b); \quad (u + v^2)^2(u - v^2)^2 - (u^2 - v^4)^2. \quad [a^2; 0]$$

$$73. (t^2 - 1)(1 + t^2) - (t^2 - 2)^2 + [(t + 1)(t - 1)]^2 - (t^2 - 2)(t^2 + 2). \quad [2t^2]$$

$$74. (m^4z^4 + n^2)^3 - 3(m^4nz^4)^2 - (m^6z^6 + n^3)(m^6z^6 - n^3) - 3(mnz)^4 - 3n^6. \quad [-n^6]$$

$$75. (x + y + z)^2 + (x + y - z)^2 + (x - y + z)^2 + (-x + y + z)^2 - 4(x^2 + y^2 + z^2). \quad [0]$$

$$76. (a^2 - 4b^2 + b^4)^2 - (a^2 + b^4)^2 - 8b^2(a + b^2)(a - b^2) + (4ab - b^4)(4ab + b^4). \quad [16b^4 - b^8]$$

$$77. \left(\frac{1}{2}a + \frac{9}{8}ab^2 - 1\right)(2a + 3) - \left(a + \frac{3}{2}ab\right)^2 - 3ab\left(\frac{9}{8}b - a\right). \quad \left[-\frac{1}{2}a - 3\right]$$

$$78. (m + 2mn + n^3)^2 - 4mn\left(m + \frac{1}{2}n^2 + n^3\right) - n^4(n^2 - 4m^2) + (m - 2mn^2)^2. \quad [2m^2 + 8m^2n^4]$$

$$79. [(2x + a)(a - 3b) - (x + a)^2 + 2b(a + 3x)]^2 - (-ab)^2. \quad [x^4 + 2abx^2]$$

$$80. (x^2 + y)(y - x)(x^2 + x) - (xy^2 - x^4)(x + 1) - x^2y[(x + 1)^2 - (2x + 2)]. \quad [0]$$

$$81. \left[\left(\frac{1}{2}a - 1 \right)^2 - \frac{1}{4}a^2 \right]^2 \cdot (1 + a)^2 - \left[a^2 - \left(\frac{1}{2} - a \right)^2 - \frac{7}{4} \right]^2 \cdot (a + 2)^2. \quad [3(2a^2 - 5)]$$

$$82. (a + b + c)^2 + (a - b)^2 + (a - c)^2 + (b - c)^2 - 3(b^2 + c^2). \quad [3a^2]$$

$$83. [(a + b + c)^2 + (a + b - c)^2][(a - b + c)^2 - (a - b - c)^2] - 8c(a - b)[(a + b)^2 + c^2]. \quad [0]$$

$$84. \left(\frac{2}{3}x^2 + y^2 \right)^3 + \left(\frac{2}{3}x^2 - y^2 \right)^3 - \frac{4}{3}x^2 \left(\frac{2}{3}x^2 + y^2 \right) \left(\frac{2}{3}x^2 - y^2 \right) - \frac{10}{3}x^2y^4. \quad [2x^2y^4]$$

$$85. \left(\frac{1}{2}x + 2xy \right) (2x + 3xy + 2y) - 2x^2y^2 - (x + 2xy)^2 - xy(1 + 4y). \quad \left[\frac{3}{2}x^2y \right]$$

$$86. (x + y + z)^2(x + y - z)^2 - [(x + y)^2 + z^2]^2 + 4z^2(x + y)^2. \quad [0]$$

$$87. (4x^2 + y^2)^2 - [(-2x + y)(2x + y)]^2 - (-4xy - 1)(-4xy + 1). \quad [1]$$

$$88. [(1 - x + x^2 - x^3)(x + 1) + (x + 1)(x - 1)(x^2 + 1)]^3 - x^3 + (2 + x)(x^2 - 2x + 4). \quad [8]$$

$$89. [(2xy - 3x^2y^2)^2 - (4x^2y^2 + 1)(1 + 9x^4y^4) + (6x^3y^3 + 1)^2]^3. \quad [0]$$

$$90. (m^3 + 2n)(m^3 - 2n) + (2n + m^2)^2 - (-2m)^2n + m^4(m + 1)(m - 1). \quad [2m^6]$$

$$91. (2mn + m^2)^3 - 4m^3n^2(2n + 3m) - m^5(m + 5n) + 4m^5n. \quad [5m^5n]$$

$$92. [(x + y)^2 - (x - y)^2]^1 - (2x + y)^2 + (y + 1)^2 + (2x + 1)(2x - 1). \quad [2y]$$

$$93. \left[\left(\frac{1}{3}a + \frac{2}{3}b \right)^3 - \frac{1}{9}ab(2a + 4b) - \frac{8}{27}b^3 \right] (3a) + \left(b^2 - \frac{1}{3}a^2 \right) \left(b^2 + \frac{1}{3}a^2 \right). \quad [b^4]$$

$$94. (t - 1)^3(t + 1)(t^2 + 1) - (t + 1)^3(t - 1)(t^2 + 1) + 4t^5. \quad [4t]$$

$$95. 2 \left(2a - \frac{b}{2} \right) \left(2a + \frac{b}{2} \right) + (b + 2c)(b - 2c) + 2(c + 2a)(c - 2a). \quad \left[\frac{b^2}{2} - 2c^2 \right]$$

$$96. \{ [(-a - 2b)(-a + 2b)(a^2 + 4b^2) + 17b^4](a^4 - b^4) + b^8 \}^2. \quad [a^{16}]$$

$$97. [(p + 2q - 1)(p - 2q + 1) + (2q - 1)^2 + 1](p^2 - 1) + 1. \quad [p^4]$$

$$98. (a^2 + b^2 - ab)(a^2 + b^2 + ab + a + b) - (a^2 + b^2)^2 - (a + b)(a^2 + b^2 - ab). \quad [-a^2b^2]$$

$$99. [4a^2 + (a + 1)^2(a - 1)^2 - (a^2 + 1)^2](a + b)^3 + a^3 + b^3 + 3ab(a + b) - (a + b)^3. \quad [0]$$

$$100. \left(\frac{1}{2}x + xy \right)^2 - \left(\frac{1}{2}x \right)^2 - x^2[(y + 1)^2 - (y + 1)] + \frac{2}{3}x[y(x + y)(x - y) + y^3]. \quad \left[\frac{2}{3}x^3y \right]$$

$$101. [(2m + an)^3 - 6am(2mn + an^2)]^2 + 2(-2amn)^3 - (8m^3 - a^3n^3)(8m^3 + a^3n^3). \quad [2a^6n^6]$$